## Supplementary information 1. Why at least 20 residue type categories are required for robust analysis of evolution on inner tree branches?

This Supplement shows the effects of categories number reduction from 20 (20 categories of residue solvent accessibilities or 20 canonical amino acids) to 8 (secondary structure types). All effects demonstrated in this Supplement can be explained by the reduction of visible mutation numbers.

The comparisons of median lengths (obtained by random delete-half-jackknifing of alignments) of inner branches of all analyzed 512 protein trees obtained based on residue solvent accessibilities ( 20 residue categories) and secondary structures ( 8 residue categories) analyses demonstrated in Fig. S1.1 and Fig. S1.2. Both heterotachy and site partitioning models show that increasing in number of branches with near zero branch lengths relates with residue categories number reduction: 2.5 fold increasing of zero-length branches in heterotachy model and 4 fold increasing of zero-length branches in site partitioning model. Additionally, the reduction of residue categories number relates with total inner branch lengths shortening.


Fig. S1.1 Lengths of inner tree branches in trees based on residue solvent accessibilities (blue) and secondary structures (orange) analyses, heterotachy model.

$\log 10$ (inner median branch length)
Fig. S1.2 Lengths of inner tree branches in trees based on residue solvent accessibilities (blue) and secondary structures (orange) analyses, site partitioning model.

Figure S1.3 shows interquartile range (Q3-Q1) of the $\ln (L)$ measures of inner branches of all analyzed 512 protein trees under heterotachy and site partitioning models based on 8 secondary structure types. The less the residue type categories in analysis the heavier the tails of interquartile range (Q3-Q1) of the $\ln (L)$ value distributions are (compare with Fig. 3). This fact clearly demonstrates that increasing in branch length variability tightly related with the residue categories number reduction.


Fig. S1.3 Interquartile range (Q3-Q1) of the $\ln (L)$ branch measures in heterotachy $(A)$ and site partitioning (B) models.

Figure $S 1.4$ shows fraction of inner branches in all analyzed 512 protein trees with absolute median $\ln (L)$ measure $>6$ under heterotachy model based on 20 RSA and 8 secondary structure types. In order to fix incongruence between branch lengths based on analysis of amino acids and secondary structures, we used threshold of abs $(\ln (\mathrm{L}))>10$. We select this threshold because the meaningful minimum of branch length is $5 \mathrm{E}-5$ (see Construction and content), therefore the case when $\mathrm{abs}(\ln (\mathrm{L}))=10$ reflects the comparison of minimum branch length with branch length closer to maximum. Figure S1.4 clearly demonstrates that reducing number of residue type categories associated with increasing number of branches having incongruence between length obtained based on amino acid alignments analysis, and length obtained based on secondary structure alignments analysis.


Fig. S1.4 The fraction of inner branches with absolute median $\operatorname{In}(L)$ measure $>10$, heterotachy model.

Figure S 1.5 shows the same as for Figure S 1.4 but under site partitioning model. This figure do not show association between reducing number of residue type categories and increasing number of branches having incongruence between lengths obtained based on amino acids and secondary structures. This is due to significantly higher variability of $\ln (L)$ measure in site partitioning model comparing to heterotachy model (see Figures 3 and S 1.3 ). In the case of $\ln (L)$ high variability the median of $\ln (L)$ for the particular branch tends to median value for general set of $\ln (L)$ values for all branches.


Fig. S1.5 The fraction of inner branches with absolute median $\operatorname{In}(L)$ measure $>10$, site partitioning model.

